YPIR: High-Throughput Single-Server PIR with Silent Preprocessing

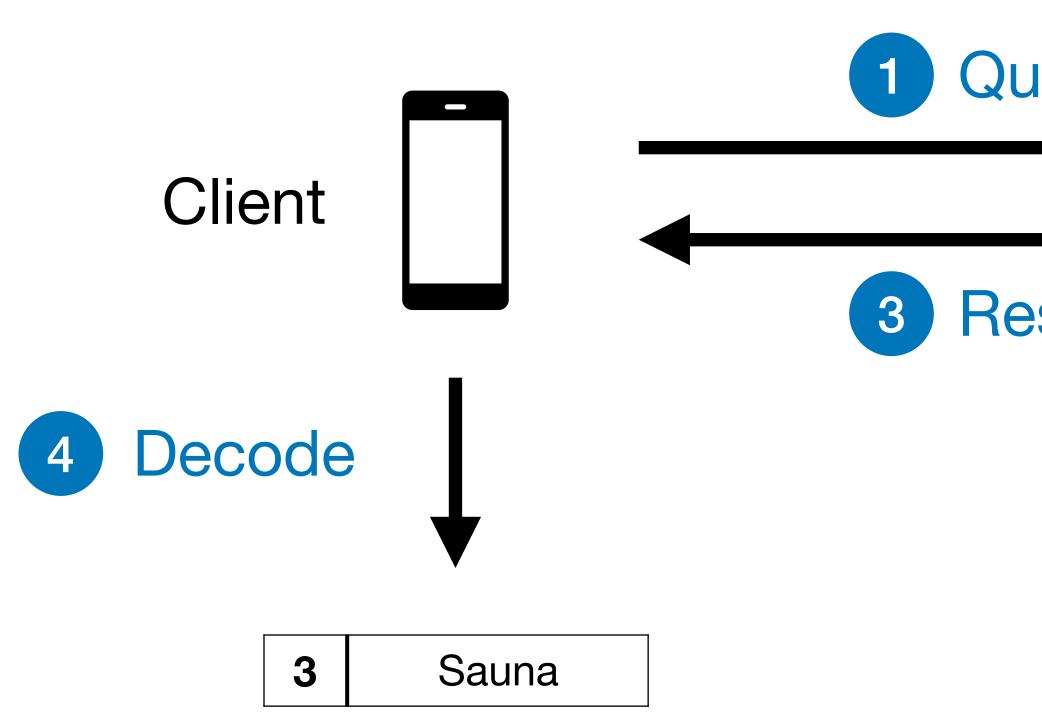
Samir Jordan Menon (Blyss) and David J. Wu (UT Austin)

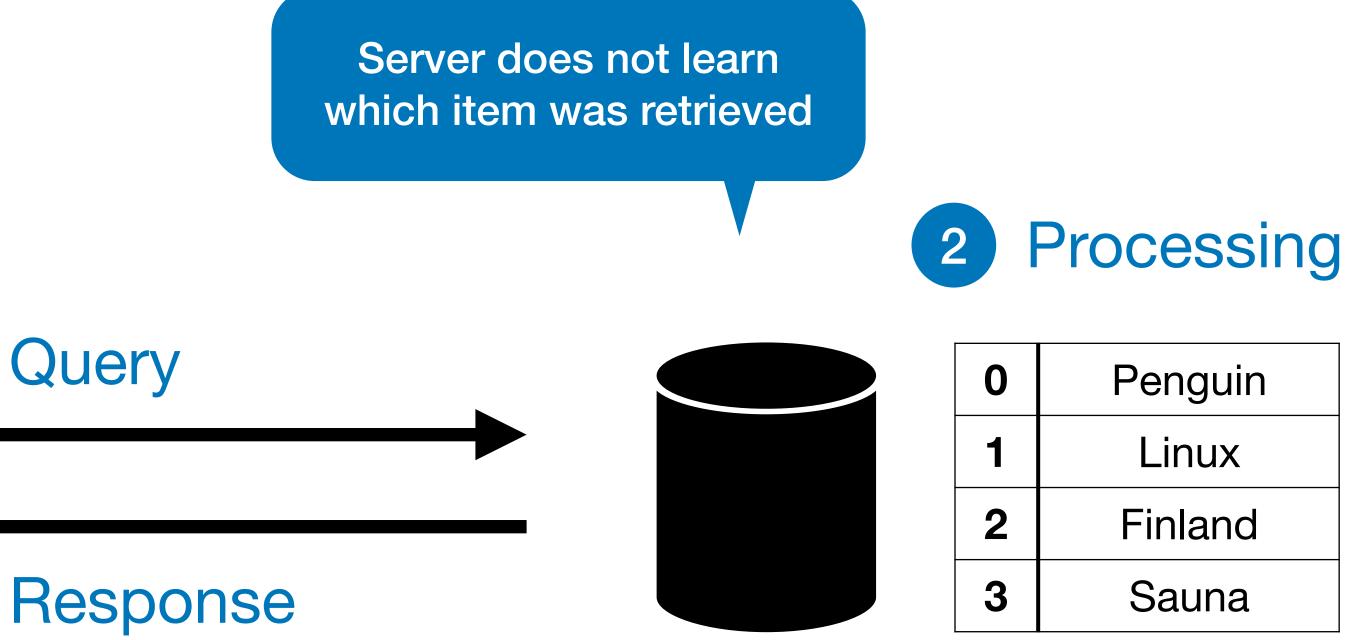
USENIX '24



[CGKS95]

Single-Server Private Information Retrieval (PIR)





Server

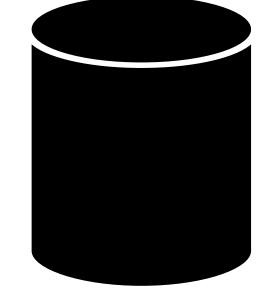
Can be used to:

- Check compromised passwords [CL24]
- Check certificate revocation [CNCW+23]
- Perform SCT auditing [HHCM+23]



Costs of SimplePIR Offline download >16 MB Goal for this work: similar costs, 360 KB without offline downloads Query size Client Response size 3 360 KB





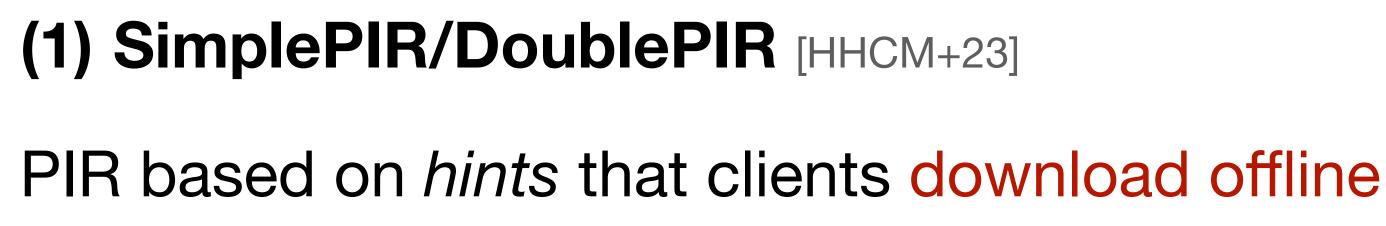
Server

0	Penguin
1	Linux
2	Finland
3	Sauna

2

11 GB/s





(2) HintlessPIR/Tiptoe = SimplePIR + hint packing [LMRS23/HDCZ23] PIR *without* offline communication, but ~10× larger responses

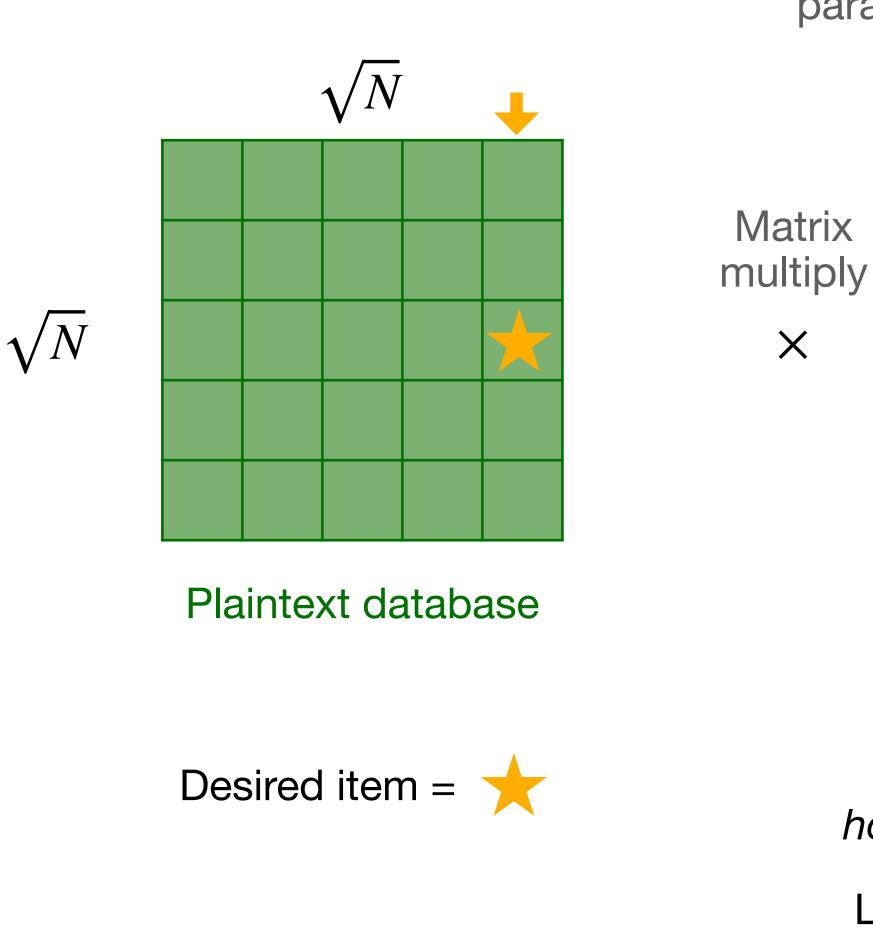
(3) YPIR (this work) = SimplePIR/DoublePIR + better hint packing

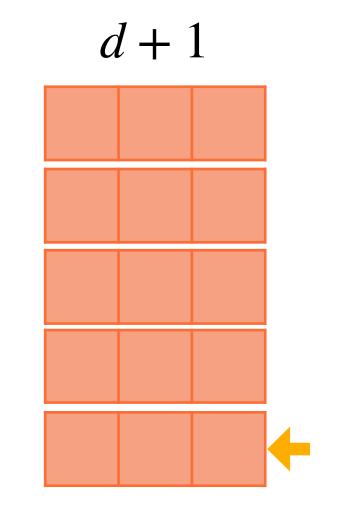
PIR without offline communication and small responses

For 1-bit retrieval: similar costs to DoublePIR, with no hints! For large item retrieval: 8× smaller responses than HintlessPIR

(1) **SimplePIR**

d depends only on the security parameter, not the database size





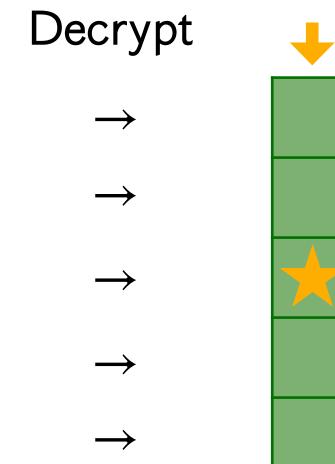
Matrix

Х

Each row is an *additively homomorphic* LWE ciphertext

Last ciphertext encrypts "1", the rest "0"

Query is $O(\sqrt{N})$



Query ciphertexts

Result ciphertexts

> Result is an encryption of the target *column* of the database, containing the item of interest

> > Response is $O(\sqrt{N})$

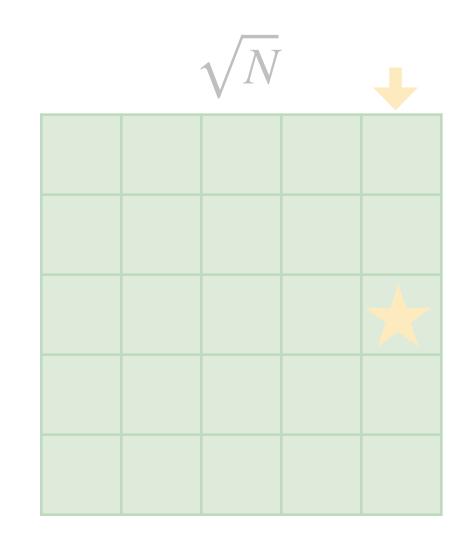




 \sqrt{N}

(1) **SimplePIR**

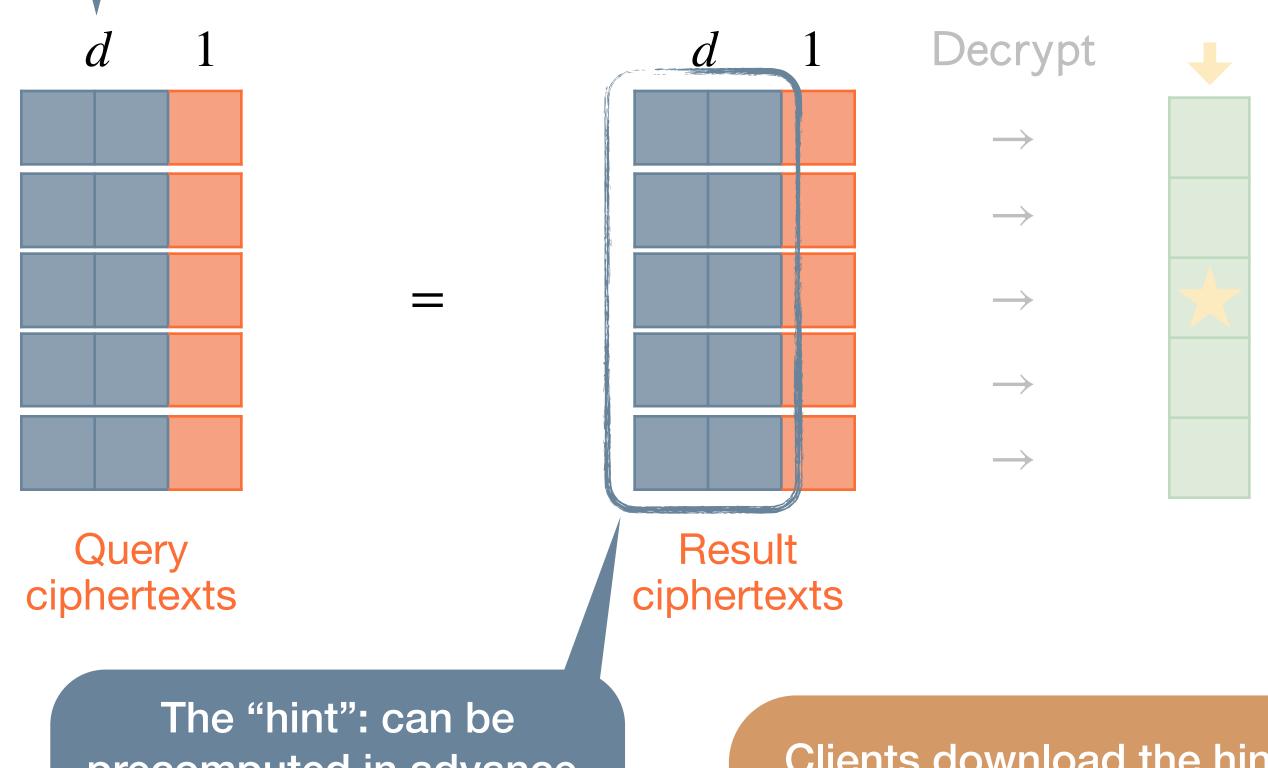
Key observation: *most* of query is pseudorandom, and can be fixed for all clients (d = 1024)

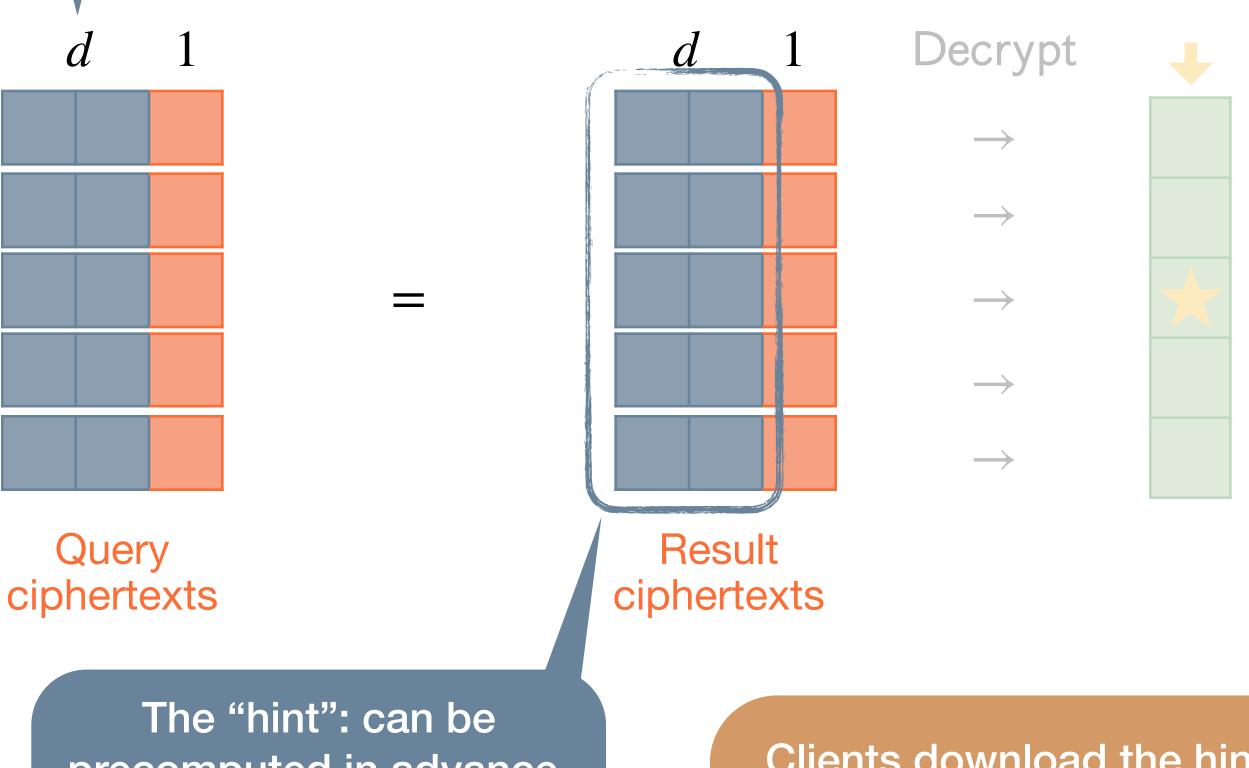


Plaintext database











precomputed in advance, and depends only on the database contents

Clients download the hint offline. Clients re-download when database updates!



(1) **SimplePIR**

The "hint": can be precomputed in advance, and depends only on the database contents

Clients download the hint offline. Clients *re-download* when database updates!

Goal for this work: similar costs, without offline downloads

Megabytes of communication to every client on every update.

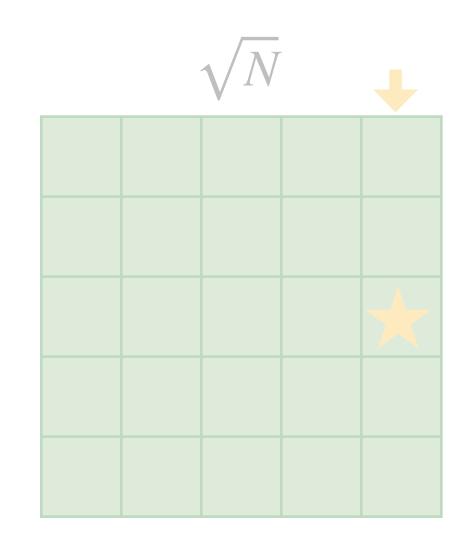
 \sqrt{N}

(1) **SimplePIR**

Matrix

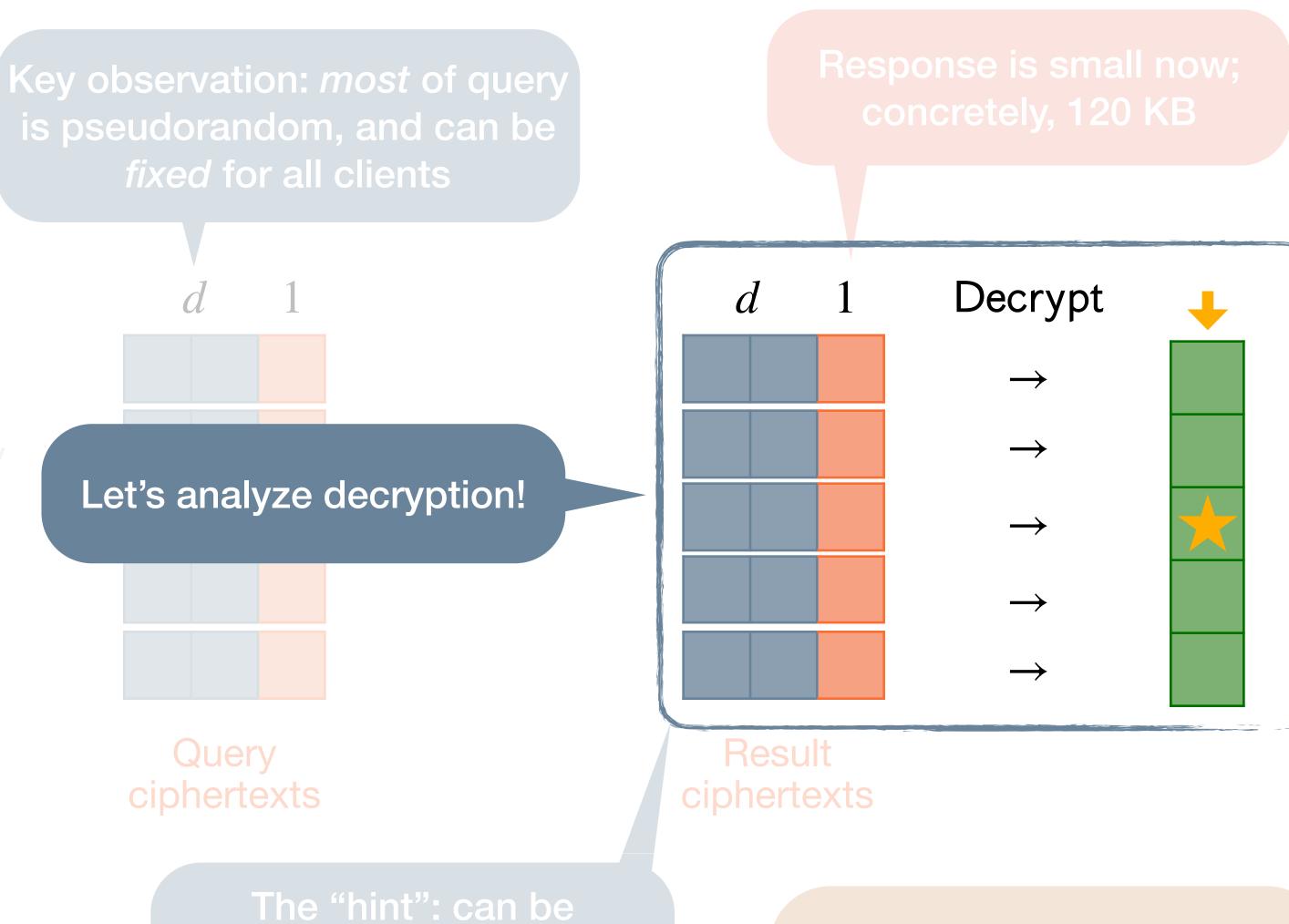
multiply

Х



Plaintext database

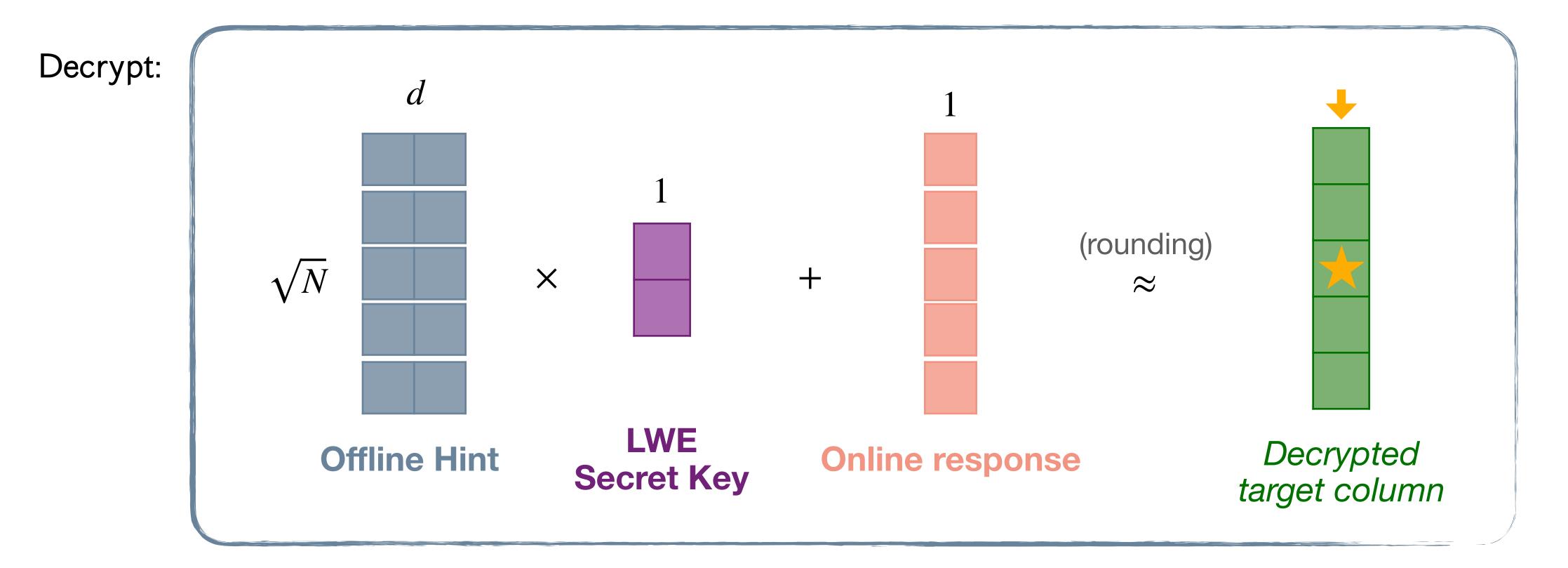




precomputed in advance, and depends only on the database contents



Analyzing decryption in SimplePIR

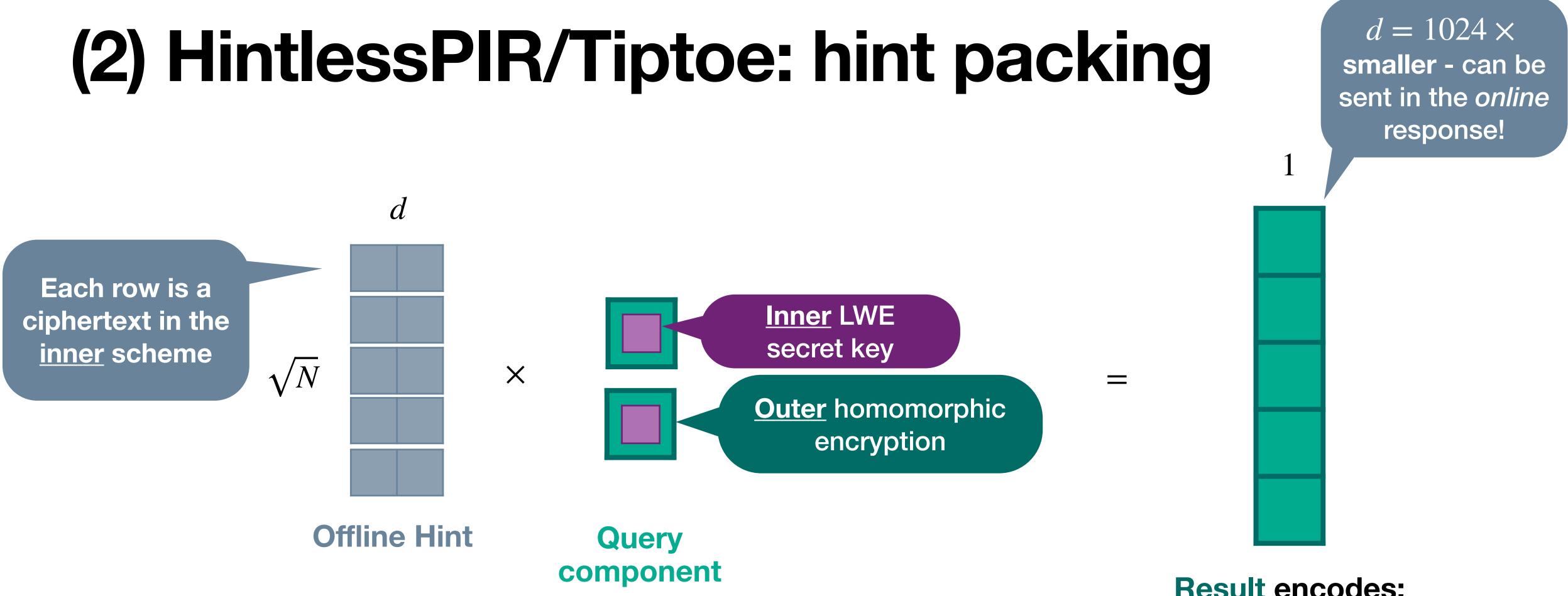


Analyzing decryption in SimplePIR



Clients don't need the whole hint to decrypt! They just need offline hint × LWE secret key. How can clients get this inner product, without communicating the entire hint?

[LMRS23, HDCZ23]

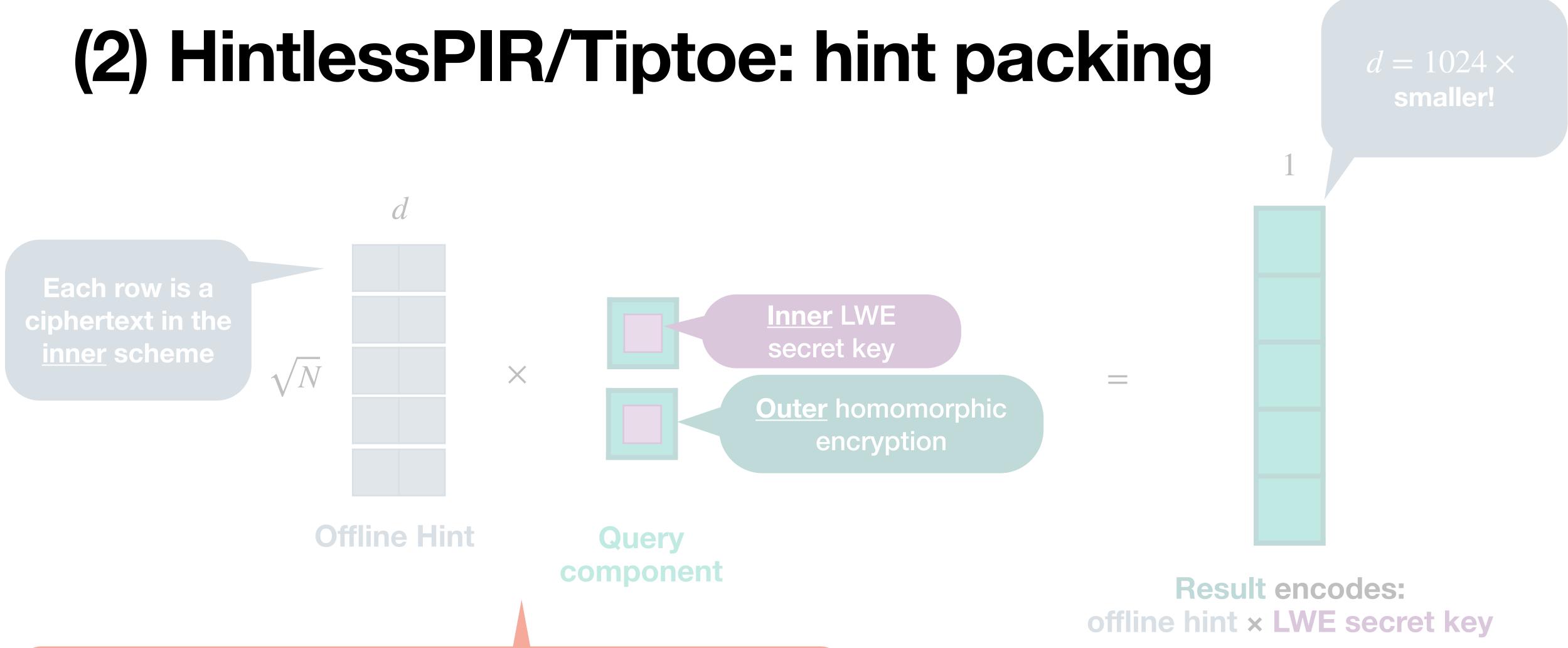


Clients encrypt their inner LWE secret vector in another, outer homomorphic encryption scheme based on Ring-LWE that is more compact

Result encodes: offline hint × LWE secret key

Server treats the hint as a plaintext, and multiplies it by the encrypted secret vector in the **outer scheme**

[LMRS23, HDCZ23]



Plaintext space of outer scheme must hold the *ciphertext* space of <u>inner</u> scheme (LWE)



Drawback: the "double wrapping" increases the response size by ~10×!



(3) YPIR: better hint packing

Prior work: Homomorphically compute LWE decryption's inner product in Ring-LWE



 \sqrt{N}

d

Yields much smaller responses

View LWE ciphertexts as 'corrupted' RLWE ciphertexts, and then perform <u>key</u> switching to uncorrupt them [CDKS21].

"Double wrapping" makes ciphertexts ~10× larger in practice

 $\approx d = 1024 \times$ smaller!

Avoid re-embedding, and just use an algebraic transform.

Ring-LWE ciphertext(s)

Also show: ~85% of work in this procedure can be moved to a onetime offline precomputation.





(3) YPIR: additional techniques

- Small item retrieval: we choose to use DoublePIR as the first phase PIR when database records are small, lowering response size from $O(\sqrt{N})$ to O(1).
- Cross-client batching: process queries from multiple clients in batching to increase effective throughput beyond the memory bandwidth limit
- Preprocessing: speed up SimplePIR preprocessing using Ring-LWE
- SCT Auditing: application of PIR to verify the correctness of a signed certificate timestamp (SCT) using a frequently-updating data structure

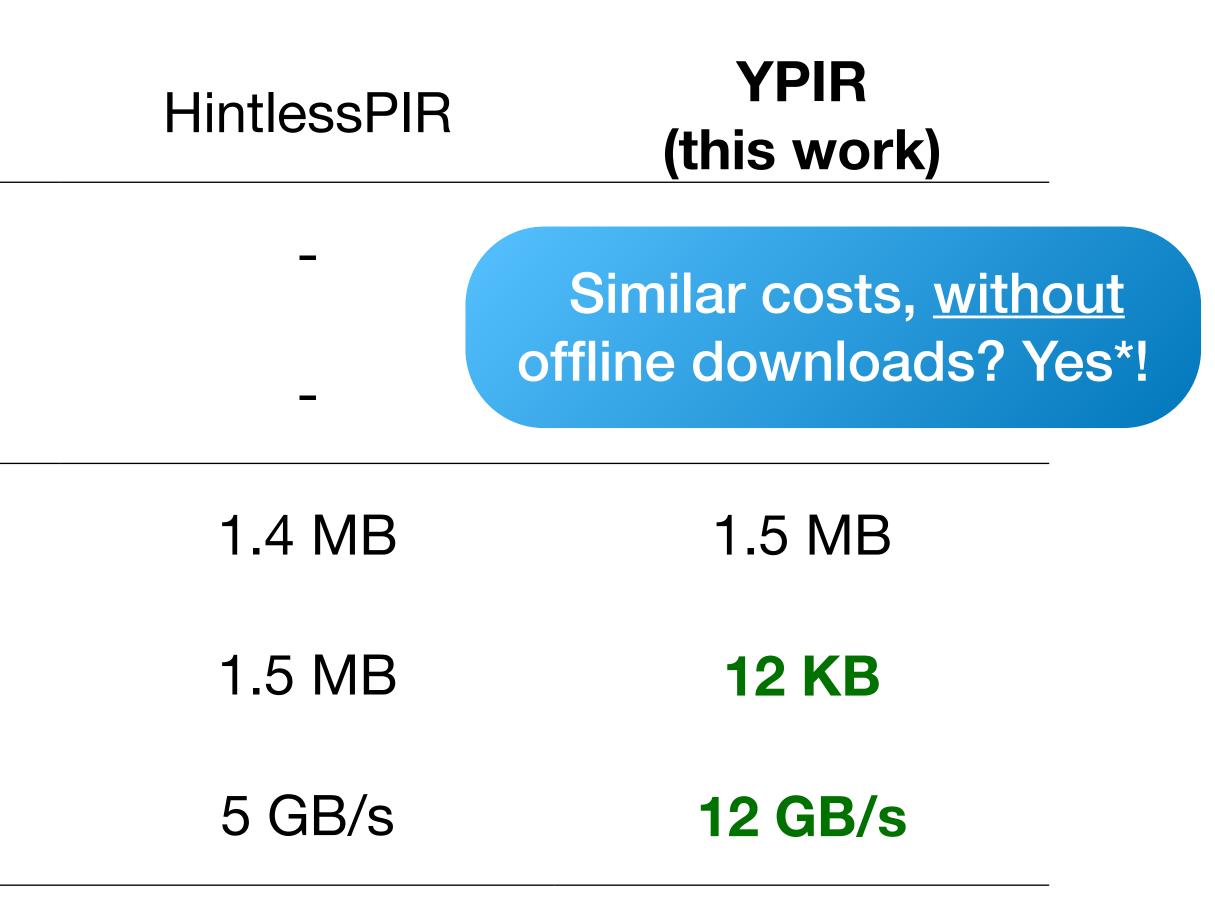
See paper for details!

Performance **1-bit retrieval from an 8 GB database**



Offline	Upload	
Offl	Download	14 MB
	Upload	1 MB
Online	Download	12 KB
U	Throughput	13 GB/s

Weekly cost to use YPIR to probabilistically check if a TLS certificate has appeared in a certificate transparency log containing 5 billion certificates is 16× lower than HintlessPIR.





Performance 32 KB retrieval from an 8 GB database

SimplePIR

Offline	Upload	
Offi	Download	362 MB
	Upload	362 KB
Online	Download	362 KB
	Throughput	11 GB/s

Check whether a password has appeared in a database of 250 million breached passwords



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YPIR+SP (this work)

1.4 MB	1.3 MB

1.7 MB
228 KB
5 GB/s
5 GB/s



Takeaways

- Offline costs matter megabytes of communication per client, per database update
- For small items, YPIR removes all offline communication from DoublePIR at little cost
- For large items, YPIR has similar throughput and query size to HintlessPIR, with smaller responses
- Replacing a bootstrapping-like approach with an algebraic solution can yield better efficiency
- Paper at <u>eprint.iacr.org/2024/270.pdf</u>, code at <u>github.com/menonsamir/ypir</u>
- Open problems:
 - Smaller queries: queries less than \sqrt{N} with high throughput
 - Silent preprocessing for PSI, ORAM, verifiable PIR



